Overview of Strategies and Methods - Division

At Gossops Green, we use the Concrete, Pictorial, Abstract method in our maths teaching. Children are simultaneously introduced to a maths concept using a range of concrete materials and equipment that they can physically manipulate, pictorial representations of a concept and more abstract ways of working. This allows for a deeper understanding of the skills and knowledge required to apply division in different contexts. An overview of these for division can be found below:

	Concrete	Pictorial	Abstract
Division	Children are taught to use the following concrete resources (the list is not exhaustive): Multilink Everyday items Place Value counters Dienes Base Ten	Children are taught to use the following pictorial representations to support their division: Drawings Part-Part-Whole Drawing arrays Number lines	Children are taught to use the following abstract methods to record / solve division calculations: Use of the ÷ symbol A B 36÷312÷3 Applying known number facts Bar model 135 5161725 Short division

Concrete **Pictorial** Abstract Explore and represent patterns within numbers up to 10, including how quantities can be distributed equally. **Sharing Sharing Sharing** Children use everyday items to share groups equally Children use pictures of everyday items to share groups Children may start to use their number knowledge to equally realise that, if they have e.g. 4 items shared between 2 children, they will get 2 each. Grouping Children are introduced to the concept of grouping through practical activities, e,g, a group of 4 children get 2 pieces of grape each

Pictorial Abstract Concrete Pupils should be taught to: halve numbers and quantities solve one-step problems involving division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher. **Sharing Sharing** Children say half of a number to 10, using their number facts knowledge. Children use multilink, counters and everyday objects Children use dots to share an amount: to manually halve or share quantities equally. Can you halve 8 cookies? **Division by sharing** objects into groups - YouTube Grouping Grouping Children start to group quantities, drawing pictures or Children place objects into groups of, e.g. 5, and see dots to represent the objects, e.g. 20 sweets divided how many groups they have: into groups of 4: Division by \$ \$ \$ \$ making groups - YouTube

Pictorial

- Calculate mathematical statements for division within the multiplication tables and write them using the division (÷) and equals (=) signs
- Solve problems involving division, using materials, arrays, mental methods, division facts, including problems in contexts. Solve problems involving division, using materials, arrays, mental methods, division facts, including problems in contexts.

Sharing

Children use concrete resources, e.g. counters, place value counters, Numicon or cubes to sort quantities into equal groups.

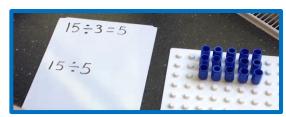
Concrete



Grouping

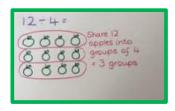
Children use counters or cubes to make arrays

<u>Division within arrays - YouTube</u>



Sharing

Children use and draw pictures or dots to pictorially share a quantity



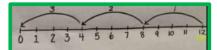
Grouping

Children draw dots in arrays



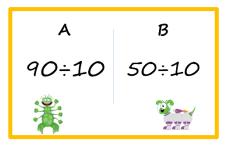
<u>Division by making groups</u> - YouTube

A number line may be used to solve division calculation as a repeated subtraction.



Children are taught related division facts for the 2, 5 and 10 times tables.

Abstract



They are taught to use the ÷ sign and to understand that it can mean 'shared' and 'grouped'.



Children interpret bar models showing divisions, e.g.

20						
5	5	5	5			

Divicion

Pictorial Abstract Concrete Pupils should be taught to: write and calculate mathematical statements for division using the multiplication tables that they know, using mental and progressing to formal written methods **Sharing Sharing** Children use their number facts to solve division calculations Children continue to make arrays, using a wider Division by sharing range of multiplication tables. I have 24 apples. If I share them amongst 3 friends, how many Children draw dots in arrays, sharing apples will each person get? 15÷3=5 36÷3 12÷3 the quantity equally. 15:5 Grouping Division by grouping have 24 apples. If I put 3 apples in a bowl, how many bowls will I Children draw dots in arrays and Grouping Children start to use short division, for then group them. calculations without remainders Children use place value counters or dienes to **Short division** two-digit number by a one digit Children draw dots to number with support their use of short regrouping division (for 2-digit numbers YouTube without remainders).

Pictorial Abstract Concrete Pupils should be taught to: Recall division facts for multiplication tables up to 12×12 Divide whole numbers by 10, 100 and 1 Use place value, known and derived facts to multiply and divide mentally Complete short division of 2-digit and 3-digit number by single digit numbers, including calculations with remainders. Children are taught the pattern for dividing whole **Sharing Sharing** numbers by 10 and 100. Children use concrete objects to demonstrate how Children draw dots to demonstrate sharing a number to divide a whole number by one. by 1: 1,000s 100s 10s 1s 0 0 ↓ ÷ 10 2 0 ↓ ÷ 10 2 1 ÷ 100 Grouping Children are taught to use short division, first **Grouping** Children draw dots to demonstrate grouping a without and then with exchanging and with number by 1: Children use place value counters or dienes to support remainders. their use of short division Short division (3 digit number by a 1 digit 12:1= 12 number) - YouTube Children draw dots to support Speed Guide to Short their use of short division. Division - YouTube

Pictorial

Pupils should be taught to:

divide numbers mentally drawing upon known facts

Concrete

- divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context
- divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context (Y6) We do not teach long division

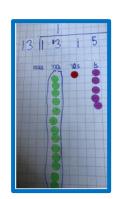
Grouping

Children use place value counters or dienes to represent the number and then use grouping to support their understanding of short division



Including when dividing by a 2-digit number



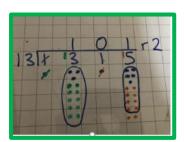


Grouping

Children use dots to represent the number and support their grouping



Including when dividing by a 2-digit number

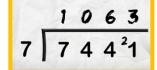


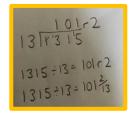
Grouping

Children continue to use short division but extending their understanding to include 4-digit numbers.

Abstract

Speed Guide to **Short Division -**YouTube





And when dividing by a 2-digit number.

Children look at the context and make decisions about how to show the remainder.

Showing remainder as a whole number:

$$\begin{array}{c|c}
8 5 8 r 2 \\
3 \overline{\smash)2^2 5^1 7^2 6} \\
\text{Answer: 858 remainder 2}
\end{array}$$

Showing remainder as a fraction: 858r2 $3 \overline{2^2 5^1 7^2 6}$

Answer: $858 \frac{2}{3}$